

Optimal Algorithms for Solution of Convex Combinations Problems

A. A. Kolpakov

University of Austin, Austin TX, USA

A. G. Kolpakov

SIBSTRIN, 234, Bld.95, 9th November str., Novosibirsk, 630009 Russia

Abstract:

We consider the convex combinations problem (CCP), which is formulated as follows: *It is required describe the set $\Lambda(\mathbf{x})$ of all coefficients of convex combinations of the given points $\{\mathbf{x}_i, i=1, \dots, n\} \in \mathbb{R}^k$ that yield the given point $\mathbf{x} \in \mathbb{R}^k$.* Using specific of the CCP, we develop an effective method for solution this problem. In particular, the method developed is optimal with probability one. We also consider the discrete convex combinations problem (DCCP), which is formulated as follows: *It is required solve the CCP under the additional condition that the coefficients of the convex combinations take value from a given finite set.*