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Explicit Expression for Primitive Idempotents of Some Cyclic Codes and Corresponding Codes

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Abstract:

Let F be a finite field of prime power order q, where q is of the form 8 3 k+. If q is primitive root modulo p^n , then the semi-simple group algebra FG of the cyclic group G of order 8 p^n over F, where p is an odd prime and $n \ge 1$, has 8 n+ 5 primitive idempotents. Explicit expressions for these primitive idempotents are obtained. Generating polynomials, minimum distances and dimensions of the corresponding minimal cyclic codes are also obtained.

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Group algebra, primitive idempotents, cyclotomic cosets, generating polynomial.