On Minimal Cuts in Ladder Graphs

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Abstract

In this paper, we consider a *ladder graph*, denoted by L_n , which represents a planar graph with 2n vertices and 3n - 2 edges. It can be visualized as a "ladder" with n rungs, formed by connecting two parallel paths of length n with n additional edges (the rungs). We study *minimal cuts* (*min-cuts*), defined as minimal sets of edges whose removal disconnects the target from the source, in ladder graphs. The deletion of any edge from a min-cut turns it into a non-cut. We explore the structure of min-cuts in both directed and undirected versions of a ladder graph and estimate their number and sizes. We show that L_n has n^2 min-cuts of sizes from 2 to n and demonstrate the distribution of the min-cuts by their sizes. In addition, using the above results, we estimate the time complexity of the algorithm that computes st-connectedness for a probabilistic directed ladder graph (the probability that there exists a path of operating edges between the source and the target in the graph). The running time of this algorithm for a directed L_n is $O(n^5)$.

Keywords

Ladder graph, min-cut, probabilistic graph, st-connectedness.